



The Skyline Design Challenge

An island named Willingdon has just been human-made. The president of the island is searching for young, creative, and brilliant architects who can build a city in Willingdon. Your challenge is to design an original model of a skyscraper building using three-dimensional shapes that will be placed in the new city on Willingdon. The president will need to see your plans, measurements, and a model in order to consider using your design. The skyscraper must stand up on its own and should include the use of at least 3 different three-dimensional shapes. You must complete the challenge within five class periods.

Compounded - 3 or more 3d shapes -
different

A Design Portfolio- The Skyline Design

Name _____

Date 11/17/10

In this design challenge, what is the problem you need to solve? We will design a 3-D sky scraper to stand in the town of Willingdon.

Specifications are the things that my solution must do. They are the project requirements. **Constraints** are things that limit my solution. For example, a **constraint** may be how much I'm allowed to spend, or how much time I have to complete the challenge.

Fill in the chart below with the **specifications** and **constraints** for this challenge.

Specifications	Constraints
• Create 3-d sky scraper to go in city of Willingdon	• original idea / own
• must stand on it's own	• must use at least 3 3d shapes
• must make model	• must be completed within 5 class periods
• record measurements	• present
• must use at least 3 3d shapes and a model	• must see plans, measurements

Name(s) _____ Date _____

Explore three different three dimensional shapes on the FabLab Modelmaker. Make sure you can defend how they are similar/different.

Our first 3D shape triangler prism

Notes:

- sides not equal
- rectangular base
- 2 triangler sides,

Our second 3D shape Cone

Notes:

- gets skinny as go up
- circle base
- 1 side

Our third 3D shape ball

Notes:

- no sides
- no vertices
- Can't be a base for building

What are some ways that make our 3D shapes similar?

1. I have no edges

2. I have sides, not equal

What are some ways that make our 3D shapes ~~similar~~ ^{different}?

1. 1 side, 3 sides, and no side

2.

2 neat discoveries: 1. You can change the color by clicking on one of the colors icons

2. Click on icon with the arrow circling left. Click green button (on shapes corner.) Spin.

PROJECT EXTRA Take Home Assignment

Use the internet, go to the library, or take pictures of skyscrapers. In the table below, write down the names of the geometric solids you found within the skyscrapers.

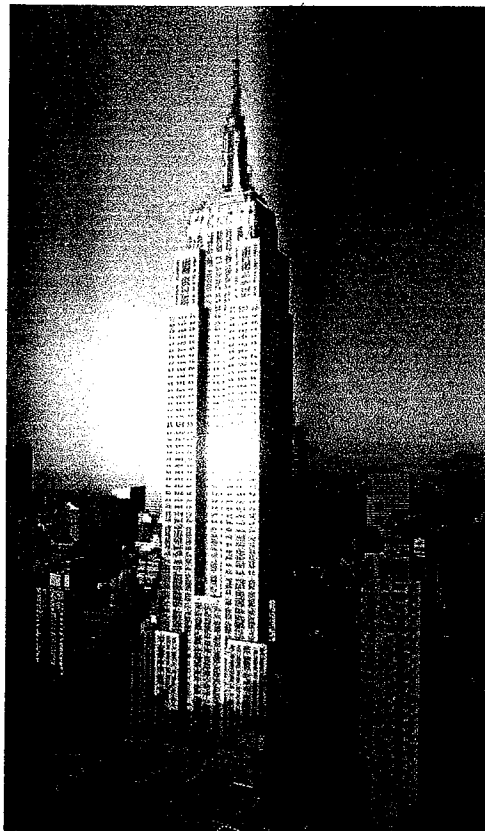
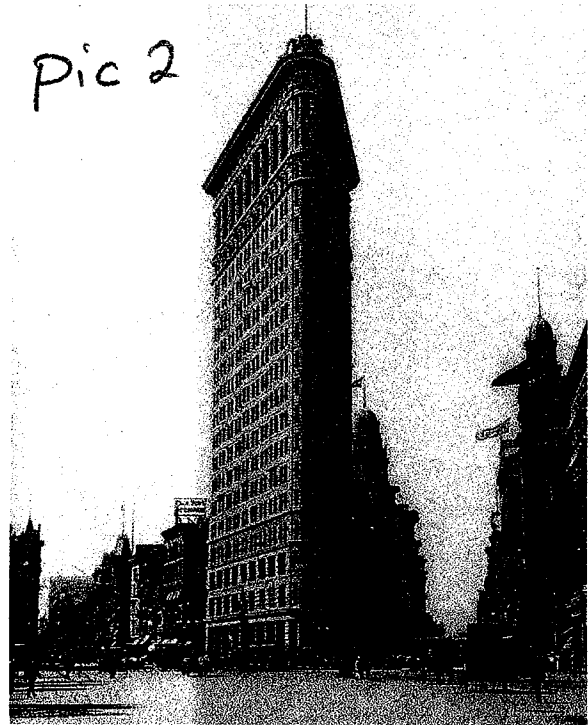
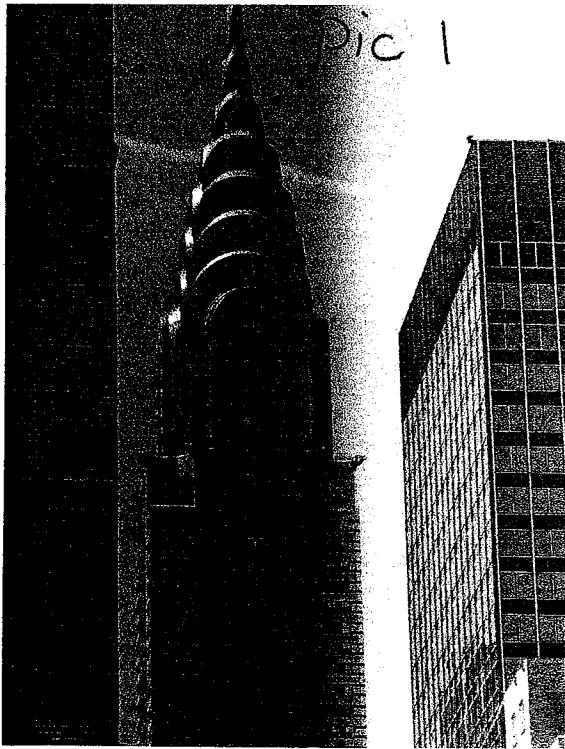
List Geometric Solids Below
• rectangular prism
• cone
• triangular prism
• cylinder
• pyramid

At least
5

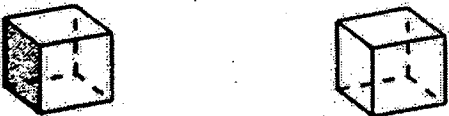






Information (3-5 bulleted observations/facts in the space below)

Pictures (3-5) based on my research (use back of this page)

- ❖ end with point (pic 1+3)
- ❖ gets skinnier as goes up (pic 1+3)
- ❖ made up of many smaller rectangular prisms (pic 3)
- ❖ 20 stories high (pic 2)
- ❖



Geometric Solids

Type		Examples	
Polyhedron	Cube		
	Rectangular prism		
	Triangular prism		
	Pyramid <i>Square pyramid</i>		
Cylinder			
Sphere			
Cone			

KSB 1 Formulating Ideas

Use the internet, go to the library, or take pictures of skyscrapers. In the table below, write down the names of the geometric solids you found within the skyscrapers.

List Geometric Solids Below

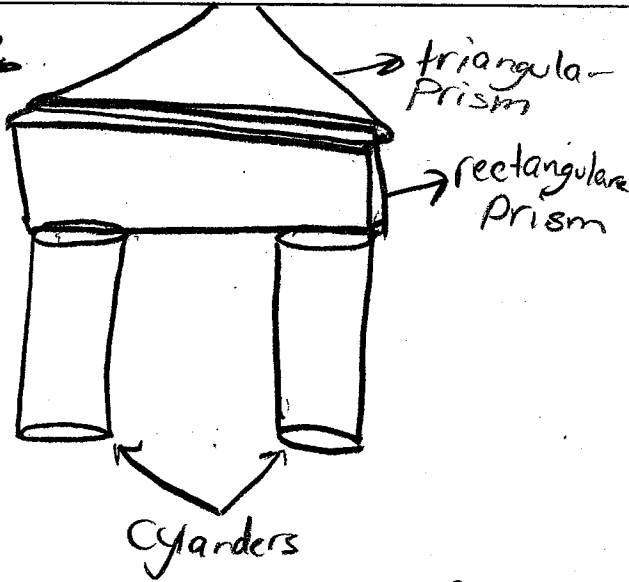
What makes a three-dimensional shape a three-dimensional shape?

11/17/10

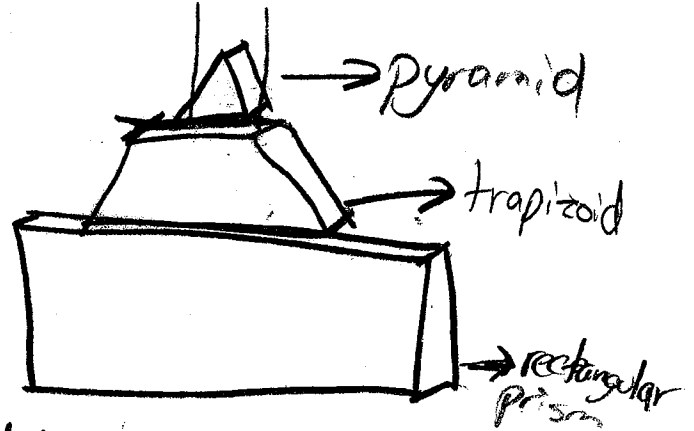
Draw two sketches of possible skyscrapers that you want to create.
Write two reasons why each sketch fulfills the specifications

Sketch 1 Individ.

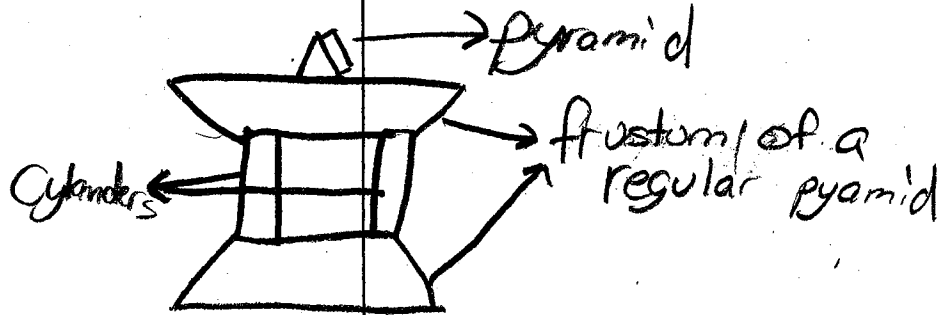
Label



Sketch 2 Individ.



Group Sketch



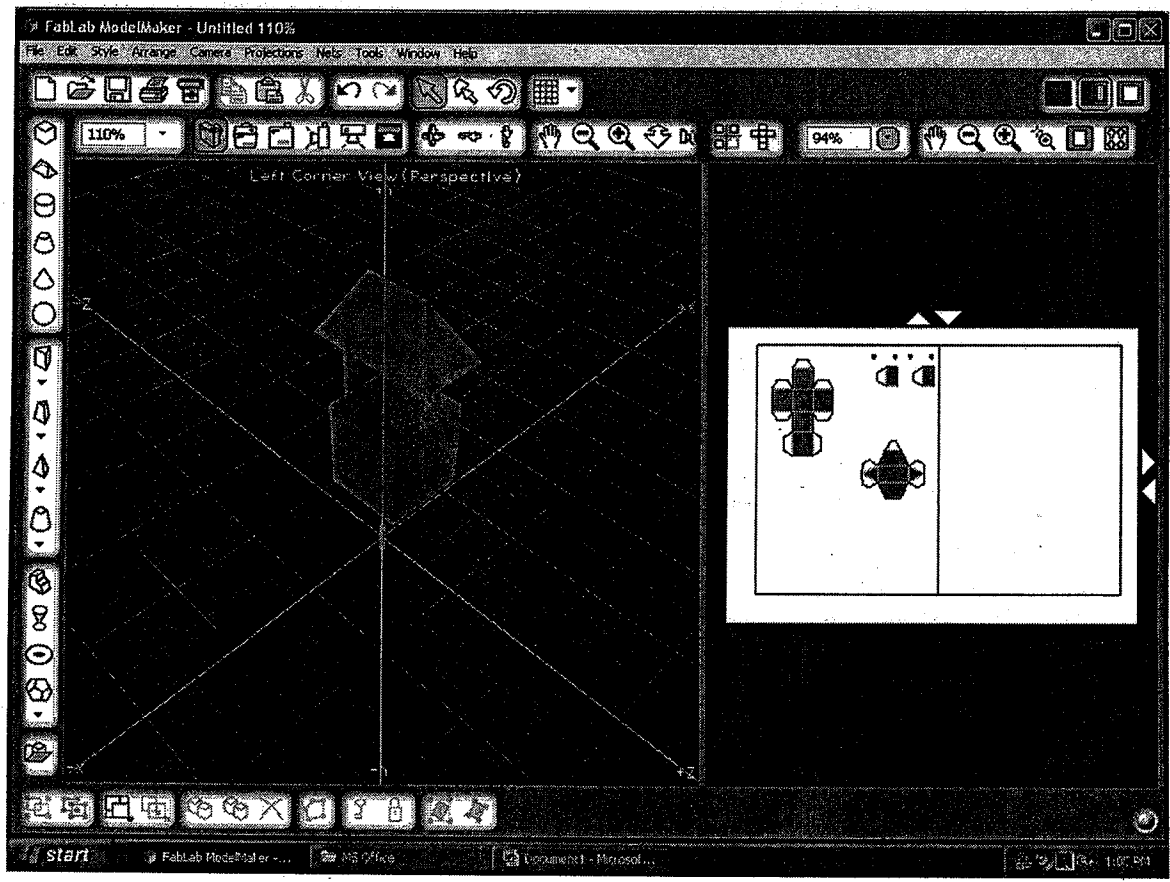
* = favorite sketch

Reason 1:

Reason 1:

Reason 2:

Reason 2:



Here Comes The Tough Part ☹️☹️☹️

Select the best skyscraper and create it using the Model Maker Software. Print the image you have on the screen. Attach the page behind this one.

The president of Willingdon has added some requirements for the model skyscraper that you're creating. Not only must the skyscraper must stand up on its own and use at least 3 three-dimensional figures, the president has requested that the skyscraper must also have a volume between 150cm^3 and 250cm^3 . The president also asked that the surface area of your model skyscraper be between 170cm^2 and 350cm^2 . In addition, you may only use a glue stick to assemble your model skyscraper. You still have 4 class periods to complete the challenge.



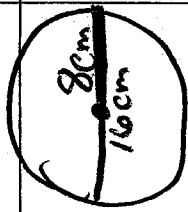
Fill in the chart below with all of the specifications and constraints for this challenge.

Specifications	Constraints
Volume be between 150cm^3 - 250cm^3	glue stick
Surface area between 170cm^2 - 350cm^2	original idea
Create 3d sky scraper	170cm^2 - 350cm^2
must stand on own	glue stick
must make model	
record measurement	
Must use at least 3 3-d shapes	

Toughfest Part 8

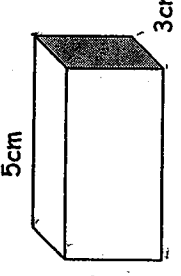
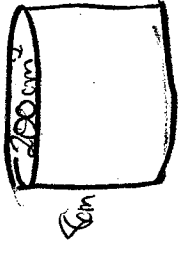

KSB 2- Surface Area

Draw each shape in the example box below. Label each shape with measurements (in centimeters) that you create. Find the area for each shape using the formulas given.




Shape	Example (Place your sketch and calculations here)	Properties of Each Shape (Ex: What makes a circle a circle?)
And Formula for Surface Area Parallelogram (square, rectangle) $A = \text{Base} \times \text{Height}$	5 centimeters  3 centimeters $A = \text{Base} \times \text{Height}$ $A = 5\text{cm} \times 3\text{cm}$ $A = 15\text{cm}^2$	
Triangle $A = (\text{Base} \times \text{Height}) \div 2$	 $A \Delta = \frac{1}{2} \text{ of Base} \times \text{Height}$ $= (\text{Base} \times \text{Height}) \div 2$ $A = 32 \div 2$ $A = 16$	
Circle $r = \text{radius}$ $r^2 = r \times r$ $\pi = 3.14$ $A = \pi r^2$	 πr^2 Diameter $\pi r = 3.14$ $r = 8$ $r^2 = 64$ $A = 64 \times 3.14$ $A = 200.96\text{cm}^2$	

KSB 3- Volume

a. The volume for the extruded figures in the chart below (rectangular prism, cylinder, triangular prism) can be determined by multiplying the area of the base by the height of the figure. Draw each three-dimensional figure in the example box. Use the measurements that you created in the surface area chart on the previous page as the measurements for the faces of the three-dimensional figures on this chart where it applies. Find the volume for each three-dimensional shape using the formulas given below.

3D Figure And Formula For Volume	Example	Properties of 3D Figure (Ex: What makes a cylinder a cylinder?)
Rectangular prism (including cube) $V = \text{Area of Base} \times \text{Height}$	 $V = \text{Area of Base} \times \text{Height}$ $V = 15\text{cm}^2 \times 2\text{cm}$ $V = 30\text{cm}^3$	Rectangular + square faces opposite faces are same area 8 vertices all right angles
Cylinder $V = \text{Area of Base} \times \text{Height}$	 $V = \text{Area} \times \text{Height}$ $V = 200\text{cm}^2 \times 8\text{cm}$ $\text{Vol } C = 1,600\text{cm}^3$	2 faces
Triangular Prism $V = \text{Area of Base} \times \text{Height}$	 $V = \text{Area} \times \text{Height}$ $V = 16 \times 20$ $\text{Vol } T = 320\text{cm}^3$	5 faces 6 vertices opposite sides equal 9 edges

24.

3D Figure	Example	Properties of 3D Figure
<p>Cone</p> <p>$V = (\text{Area of base} \times \text{Height}) \div 3$</p>	 <p>$V = 15,888 \text{ cm}^3$. 1 face $B.A. = 8,920 \text{ cm}^2$. 1 vertex $H = 5,400 \text{ cm}$. will roll</p>	
<p>Square Base Pyramid</p> <p>$V = (\text{Area of Base} \times \text{Height}) \div 3$</p>	 <p>$V = 36,468 \text{ cm}^3$. 5 faces $B.A. = 17,640 \text{ cm}^2$. 5 vertices $H = 6,200 \text{ cm}$. not roll</p>	
<p>Triangle Base Pyramid</p> <p>$V = (\text{Area of Base} \times \text{Height}) \div 3$</p>	 <p>$V = 65,19 \text{ cm}^3$. 4 faces $B.A. = 29,110 \text{ cm}^2$. 4 vertices $H = 6,800 \text{ cm}$. not roll</p>	

Which three-dimensional figure included in the chart would roll from one side of a table to the other the best? Why? The cone because it doesn't have any edges stopping it.

STOP! You must get your work checked by the teacher in order to continue

Teacher's Signature _____

KSB 4- Using ModelMaker

Open the ModelMaker software and create each of the three-dimensional figures you found the volume for on the previous pages. Use the same dimensions and units that you used in the chart above. After you create each figure, right click on it, and go to Properties. Scroll to the bottom to view the calculated volume and record it in the space provided below. Repeat for each figure you create. Print the images you have on the screen and attach it to the back of this page.

Three-dimensional Figure	Volume
Rectangular Prism	30 cm ³
Cone	15.88 cm ³
Cylinder	1600 cm ³
Triangular Prism	320 cm ³
Square Base Pyramid	36.46 cm ³
Triangle Base Pyramid	65.99 cm ³

Does the volume for each figure match the volume you calculated in the chart? If not, make sure you used the same dimensions and units in your chart example and in ModelMaker. You may also want to go over the computations in your example.

Was there a mistake? no

Which figures had a mistake? none

Where did you find the mistake? (You may want to look back to your computations for surface area and volume. Did you use the formulas correctly? Did you complete the multiplication correctly? Did you copy a number incorrectly?)

I didn't

Revised Optimum Skyscraper Design

Using Model Maker, create a revised design of the skyscraper that meets the new requests of the president of Willingdon. Print the image that you have on the screen and attach it to the back of this page. This is the design that you will be constructing.

STOP! Your teacher must approve your skyscraper design.

Teacher's Signature _____

Once your teacher signs your portfolio you may print the nets of each figure and construct your design.

Which three-dimensional figures did you use in your design?

I used two cylinders, a frustum of a regular pyramid, and a cone.

Why did you choose these figures?

We thought it would look good, and appropriate for our building idea, which is a technology museum.

In the chart below, list each three-dimensional figure that you used to create your skyscraper. Using ModelMaker, find the volume of each figure and record it in the space provided.

Three-dimensional Figure	Volume	Surface Area
Cylinder (2)	8.84	27.76 ^c
frustum of a regular pyramid	75.53	124.02
Cone	62.72	96.59

Hard

Total surface area

$$\underline{263.51 \text{ cm}^2}$$

Total volume of skyscraper

$$\underline{155.93 \text{ cm}^3}$$

Surface area work

bottom shape - 124.02	Cylinder - base 1.64
middle shapes = 27.76	$\times 2$
27.76	$\frac{3.28}{6.56}$
top shape - 96.59	213.85
$\underline{276.53}$	$\underline{- 3.28}$
$\underline{- 3.28}$	$\underline{278.07}$
$\underline{273.35}$	$\underline{- 36.56}$
	$\underline{263.51}$

Using ModelMaker and the model of your skyscraper, determine the surface area of your design. (Hint: Don't count the surface area of the faces and parts of faces that cannot be seen when the building is standing upright.)

Use the space below for your calculations.

Calculations for figure 1

cylinder
 surface area -
 27.76 cm^2
 volume - 8.84 cm^3

Calculations for figure 2

Cylinder
 surface area -
 27.76 cm^2
 volume - 8.84 cm^3

Calculations for figure 3

Cone
 surface area -
 96.59 cm^2
 volume - 62.72

Calculations for figure 4

Frustum of a
 regular pyramid
 surface area -
 124.62
 volume - 75.53

Surface area of figure 1: 27.76 cm² cm²

Surface area of figure 2: 27.76 cm² cm²

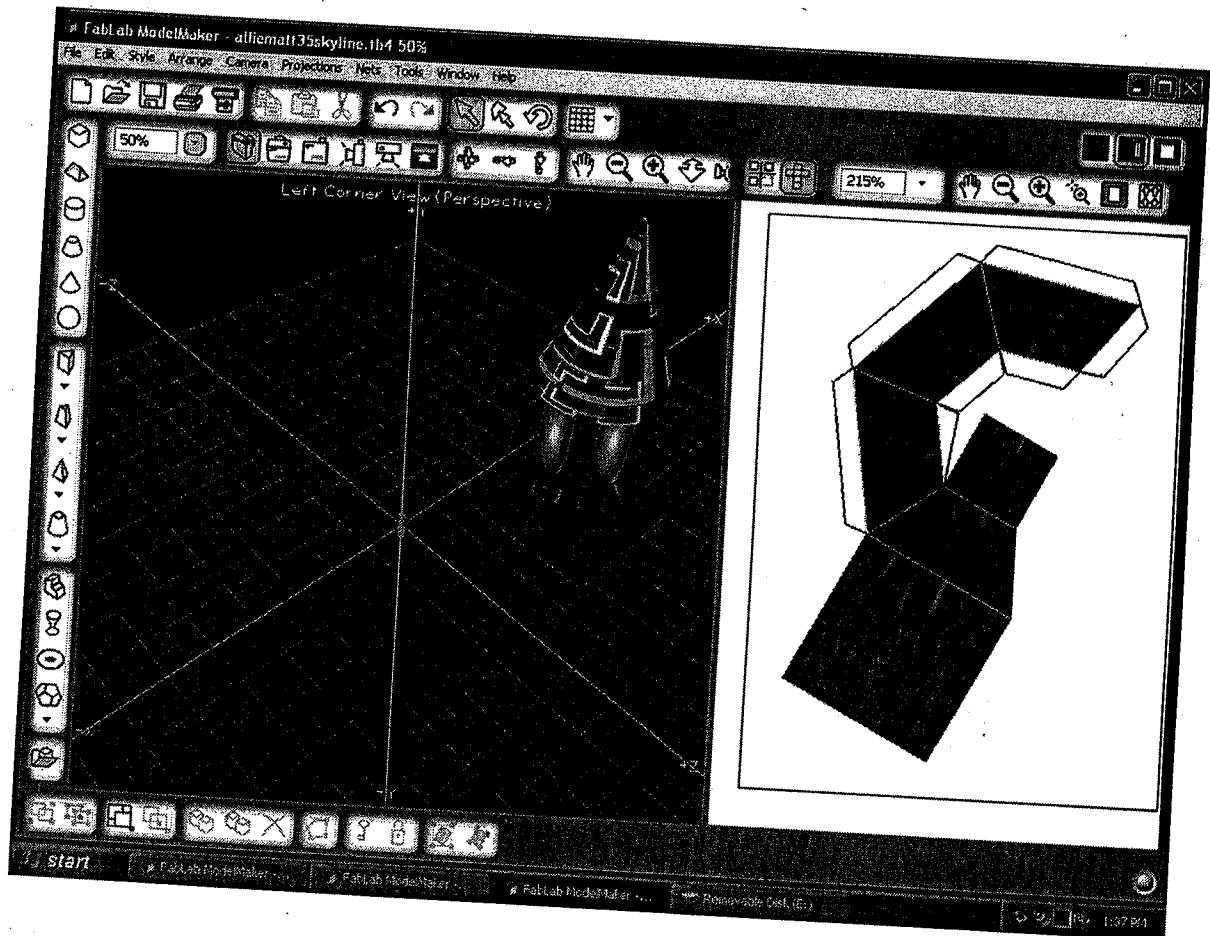
Surface area of figure 3: 96.59 cm² cm²

Surface area of figure 4: 124.62 cm²

What changes, if any, did you make from your plan of the skyscraper? Why? Did the skyscraper meet all of the specifications? Explain

When we got the second specs and constraints, we realized that our volume and surface area were over the limit. We had to change our shapes so it would meet the correct size.

Print out the screen image of your final design and paste it in the space below. Label the important features that indicate the skyscraper met the specifications.



Reflection

What did you learn about three-dimensional figures, surface area, and volume by completing this design challenge? I learned how to calculate the volume and surface area of many three-dimensional figures, such as cones, cylinders, and regular pyramids. I also learned that the equations to find surface areas and volumes are different for different figures. For example, the equation for finding the volume of a cylinder, you multiply the area by the height.

What are some trade-offs or modifications that you had to make in order to be sure that your design fit all of the specifications? We had to change our first shape we created on skyline completely, because it was way too big. Both the surface area and the volume went way out of the specs. Also, our top shape was bigger than our bottom shape, so it probably wouldn't stand on its own.

Exchange your design portfolio and model skyscraper with a neighbor. Use your peer review rubric to evaluate your partner's work. When you are finished, return the model skyscraper, design portfolio, and rubric to your neighbor. Attach the rubric that your neighbor filled out for your skyscraper to the back of your design portfolio.

$$\begin{array}{r} 54.21 \\ -12.32 \\ \hline 41.89 \end{array} \quad \begin{array}{r} 37.39 \\ -7.19 \\ \hline 30.20 \end{array}$$

Notes for question 1:
 Cube: $V: 54.21 \text{ cm}^3$, $BA: 12.32 \text{ cm}^2$
 Cylinder: $V: 37.39 \text{ cm}^3$, 7.19 cm^2
 Wedge: $V: 22.80 \text{ cm}^3$, 22.80

Extension Questions

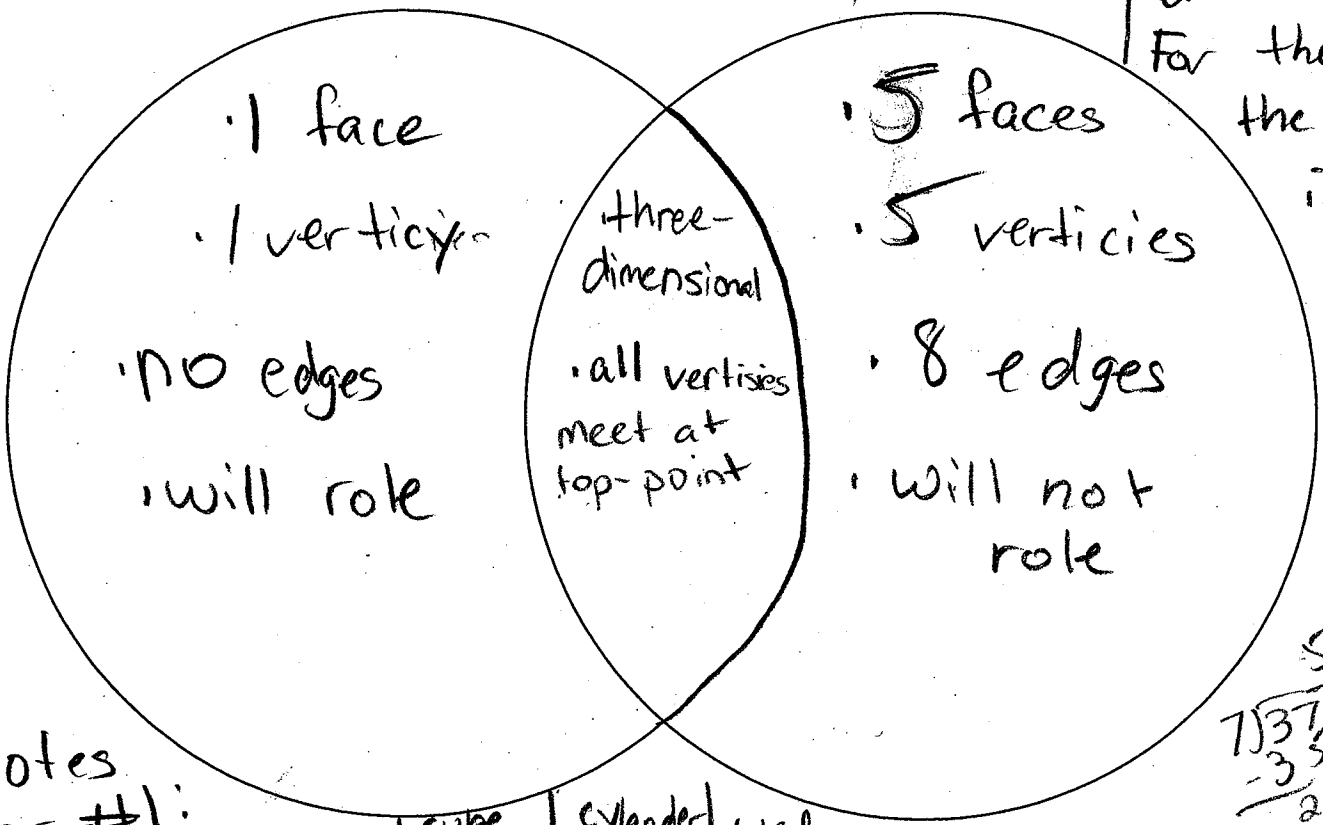
1. How does the base area of an extruded figure relate to the volume of the extruded figure? Does the way to find the relationship change for different figures. For the wedge, the volume and the base area were the same. For the cube, the volume was 41.89 cm larger than the surface area. For the cylinder, the volume was 30.20 cm bigger. If you divide the volume by the

2. Use the Venn diagram below to note the similarities and differences of a cone and a pyramid.

Cone

Square Pyramid

For the cylinder, it's about $5 \frac{2}{7}$. For the cube, the quotient is about $3 \frac{2}{3}$. For the wedge, the quotient is one.



Notes for #1:
 $12 \overline{) 154}$
 $\underline{46}$
 $\frac{33}{8}$

	cube	cylinder	wedge
V	54.21 cm ³	37.39 cm ³	22.80 cm ³
BA	12.32 cm ²	7.19 cm ²	22.80 cm ²

same

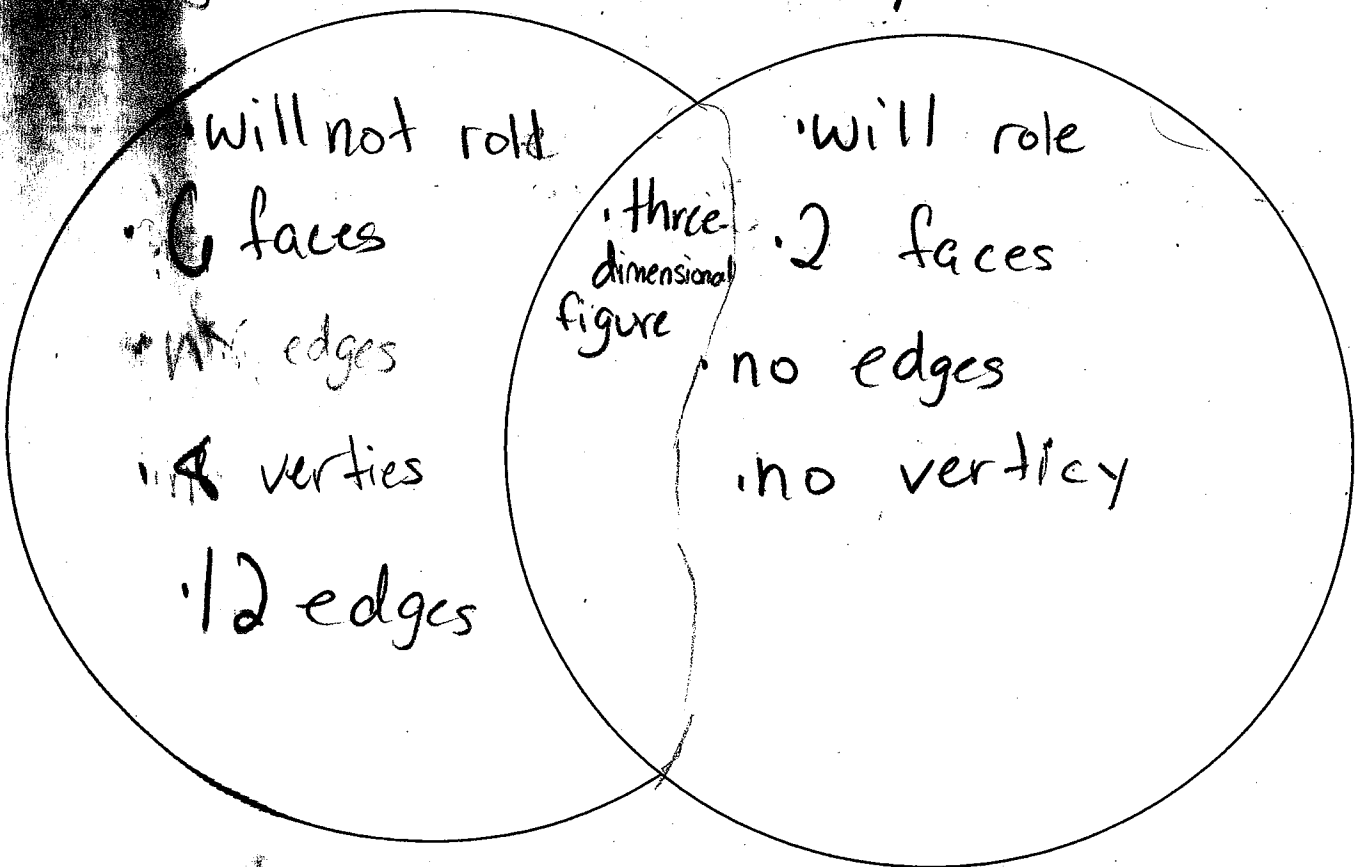
$$\begin{array}{r} 57 \\ 1137 \\ -35 \\ \hline 2 \end{array}$$

$$719 \overline{) 3739}$$

Use the Venn diagram below to compare and contrast 2 three-dimensional shapes of your choice.

Cube

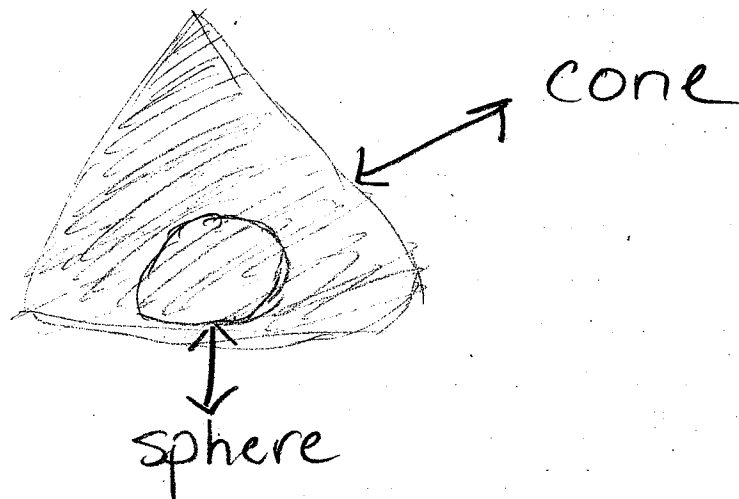
Cylinder



4. If the president of Willingdon required your unique design to include at least one three-dimensional figure placed inside another, how would you approach this? What are some things that you might think about? I

would put a sphere through cone. I would make the cone larger than the sphere. I would do this because I could first build the ball, and then easily place the sphere in the cone as I fold it. Also, if I make the sphere smaller than the cone, it will give the sphere more place to move, making it easy to put in a cone.

Sketch one possible design for this requirement.



Day _____

This is what I did today: _____

This is what I learned: _____

Day _____

This is what I did today: _____

This is what I learned: _____

Day _____

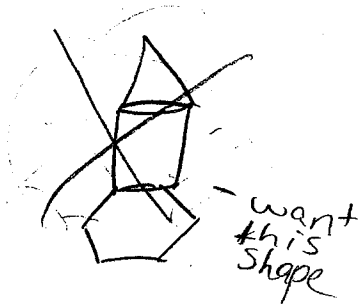
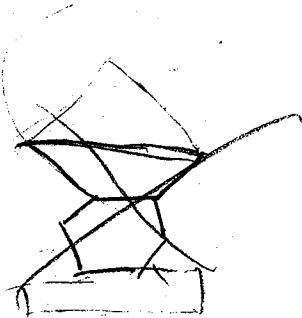
This is what I did today: _____

This is what I learned: _____

11/3/10

idea - office building + tourist attraction

- small cylinder or cone at top
- tall / big
- skinny
- hexagon
- combine all ideas



idea - similar to the cristlar

- war company building
- really unusual shape - tourist attraction
- cone + cylinder

Notes

18.84
 + 8.84

 115.68
 + 75.53

 93.21



0 1490
 x 50.00

 93.21

 56.79

+ 221.21
 - 85.52

 246.73

196.59
 + 124.62

 221.21

127.76
 + 27.76

 55.52